Аномалии, гидродинамика и эффективная гравитация

Летняя школа Фонда «БАЗИС» — 2023 «Квантовые поля: от гравитации и космологии до физики конденсированного состояния»

1 августа 2023 г.

Олег Теряев

Объединенный институт ядерных исследований, Дубна МГУ им. М.В. Ломоносова, Москва (каф. Физики элементарных частиц, Филиал МГУ в Дубне) Что связывает самые сильные (КХД) и самые слабые (гравитация) взаимодействия?

- Адронные матричные элементы оператора тензора энергии импульса (ТЭИ) описывают взаимодействие с классической гравитацией и жесткие процессы в КХД
- При столкновениях тяжелых ионов возникает среда, движущаяся с максимальными из когдалибо наблюдавшихся ускорениями и завихренностями (локальными угловыми скоростями, что согласно принципу эквивалентности соответствует сверхсильной (эффективной) гравитации

КХД и гравитация (продолжение)

- В термализованной кварк-глюонной среде возникают квантовые эффекты (Унру: квантовое измерение в ускоренной системе отсчета), соответствующие (эмерджентной) конической сингулярности: связь термальной и гравитационной потери информации?
 - Гравитационная квантовая аномалия порождает термальные эффекты, сохраняющиеся после ее исчезновения
 - Fолография:AdS/QCD



Main Topics

- Equivalence Principle: way to merge strongest and weakest interactions
- Gravitational Formfactors: EP for spin and its Extension
- D-term, pressure and inflation
- Spin-1 and average shear
- Heavy ion collisions : highest vorticity and acceleration
- Anomalous current and polarization (EFT/TD/Gravity)
 Unruh radiation

Strong interactions and gravity

- $E_{EM}/E_G \sim e^2/(m/M_{Pl})^2$ $M_{Pl} \sim 10^{18} \text{ GeV}$
- For 2 particles with M_{Pl} mass at Compton wavelength distance $(1/M_{Pl})$: $E_G \sim (G = 1/M_{Pl}^2) M_{Pl}^2 / (1/M_{Pl}) = M_{Pl}$ g ~ $(G = 1/M_{Pl}^2) M_{Pl} / (1/M_{Pl})^2 = M_{Pl}$
- Gravitational interaction is strongly suppressed $\sim (\Lambda/M_{\textrm{Pl}})^2$
- Equivalence Principle
- I: Acceleration <-> Gravity
- HIC: a ~ Λ , a/g ~ $\frac{c^2}{v_{\oplus}^2} \cdot \frac{R_{\oplus}}{R_A}$ ~ 10³⁰
- M_{Pl} -> Λ ("GeV Gravity")
- Coupling to Energy-Momentum Tensor

Electromagnetism vs Gravity (OT'99)

- Interaction field vs metric deviation
- $M = \langle P' | J_q^{\mu} | P \rangle A_{\mu}(q) \qquad M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$ Static limit
- $\langle P|J^{\mu}_{q}|P\rangle = 2e_{q}P^{\mu} \qquad \qquad \sum_{q,G} \langle P|T^{\mu\nu}_{i}|P\rangle = 2P^{\mu}P^{\nu} \\ h_{00} = 2\phi(x)$

$$M_0 = \langle P | J_q^{\mu} | P \rangle A_{\mu} = 2e_q M \phi(q) \qquad M_0 = \frac{1}{2} \sum_{q,G} \langle P | T_i^{\mu\nu} | P \rangle h_{\mu\nu} = 2M \cdot M \phi(q)$$

Mass as charge – equivalence principle

EP and hadron structure

- "Microscopic" EP (coupling of gravity to EMT)
- +
- Conservation law (Momentum SR to get local from LC pdf's): ∫dx x (Σ q(x) + G(x))=1)
- =
- Macroscopic" EP (universal falling) :
- Tested VERY precisely

Gravitational Formfactors (Pagels'66, Ji'97)

 $\langle p'|T^{\mu\nu}_{q,g}|p\rangle = \bar{u}(p') \Big[A_{q,g}(\Delta^2) \gamma^{(\mu} p^{\nu)} + B_{q,g}(\Delta^2) P^{(\mu} i \sigma^{\nu)\alpha} \Delta_{\alpha}/2M] u(p)$

Conservation laws - zero Anomalous Gravitomagnetic Moment : $\mu_G = J$ (g=2)

 $P_{q,g} = A_{q,g}(0) \qquad A_q(0) + A_g(0) = 1$

 $J_{q,g} = \frac{1}{2} \left[A_{q,g}(0) + B_{q,g}(0) \right] \qquad A_q(0) + B_q(0) + A_g(0) + B_g(0) = 1$

- No M_{Pl}! May be extracted from high-energy experiments/NPQCD calculations
- Describe the partition of angular momentum between quarks and gluons Ji's SRs
- Describe interaction with both classical and TeV gravity

Ji's and 1st moment "mass" SRs: Generalized Parton Distributions imply models for both EM and Gravitational Formfactors (Selyugin,OT '09)

■ Smaller mass square radius (attraction vs repulsion ☉): follows from Regge behaviour of GPDs ~ x^{a(t)} (cf AdS QCD)

$$\rho(b) = \sum_{q} e_{q} \int dxq(x,b) = \int d^{2}qF_{1}(Q^{2} = q^{2})e^{i\vec{q}\cdot\vec{b}}$$

$$= \int_{0}^{\infty} \frac{qdq}{2\pi} J_{0}(qb) \frac{G_{E}(q^{2}) + \tau G_{M}(q^{2})}{1 + \tau}$$

$$\rho_0^{\rm Gr}(b) = \frac{1}{2\pi} \int_\infty^0 dq q J_0(qb) A(q^2)$$

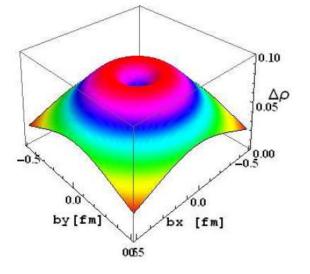


FIG. 17: Difference in the forms of charge density F_1^P and "matter" density (A)

Gravitomagnetism

Gravitomagnetic field (weak, except in gravity waves) – action on spin from $M = \frac{1}{2} \sum_{q,G} \langle P' | T_{q,G}^{\mu\nu} | P \rangle h_{\mu\nu}(q)$ $\vec{H}_J = \frac{1}{2} rot \vec{g}; \ \vec{g}_i \equiv g_{0i}$ spin dragging twice

• Lorentz force – similar to EM case: factor $\frac{1}{2}$ cancelled with 2 from $h_{00} = 2\phi(x)$ Larmor frequency same as EM

$$\omega_J = \frac{\mu_G}{J} H_J = \frac{\omega_L}{2} = \omega_L \vec{H}_L = rot \vec{g}$$

Spin momenta dragging – the same -

 Orbital and Spin momenta dragging – the same -Equivalence principle

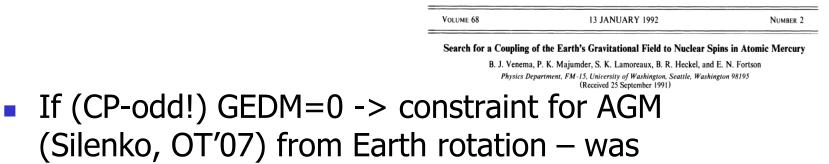
Equivalence principle

- Newtonian "Falling elevator" well known and checked (also for elementary particles)
- Post-Newtonian gravity action on (quantum!) SPIN – known since 1962 (Kobzarev and Okun'; ZhETF paper contains acknowledgment to Landau: probably his last contribution to theoretical physics before car accident); rederived from conservation laws -Kobzarev and V.I. Zakharov
- Anomalous gravitomagnetic (and electric-CPodd) moment iz ZERO or
- Classical and QUANTUM rotators behave in the SAME way

Experimental test of PNEP

Reinterpretation of the data on G(EDM) search

PHYSICAL REVIEW LETTERS



- considered as obvious (but it is just EP!) background
- New high precision EDM experiments: gravity is essential (NN Nikolaev, Vergeles, Silenko,...)

$$\mathcal{H} = -g\mu_N \boldsymbol{B} \cdot \boldsymbol{S} - \zeta \hbar \boldsymbol{\omega} \cdot \boldsymbol{S}, \quad \zeta = 1 + \chi$$

 $|\chi(^{201}\text{Hg}) + 0.369\chi(^{199}\text{Hg})| < 0.042$ (95%C.L.)

EP and quantum measurement

- If spin is just a geometric vector, EP for Earth's rotation is "trivial": spin rotates with Earth's angular velocity like Foucault pendulum
- Non-trivial if quantum measurement (quite practical here) is performed in the rotating frame

Equivalence principle for moving particles EPII vs EPI

- Compare gravity and acceleration: gravity provides EXTRA space components of metrics
- Matrix elements DIFFER $h_{zz} = h_{xx} = h_{yy} = h_{00}$

 $\mathcal{M}_g = (\epsilon^2 + p^2) h_{00}(q), \qquad \mathcal{M}_a = \epsilon^2 h_{00}(q)$

- Ratio of accelerations: $R = \frac{\epsilon^2 + p^2}{\epsilon^2}$ confirmed by explicit solution of Dirac equation (Silenko, OT, '05)
- Arbitrary fields Obukhov, Silenko, OT '09,'11,'13,16,17: also the same dynamocs for classical and quantum rotators ("EP for strong fields")

Gravity vs accelerated frame for spin and helicity

- Spin precession well known factor 3 (Probe B; spin at satellite – probe of PNEP!) – smallness of relativistic correction (~P²) is compensated by 1/ P² in the momentum direction precession frequency
- Helicity flip the same!
- No helicity flip in gravitomagnetic field another formulation of PNEP (OT'99) and
- Flip by "gravitoelectric" field: relic neutrino (Anisotropic Universe: Kamenshchik,OT'15)? Black hole?

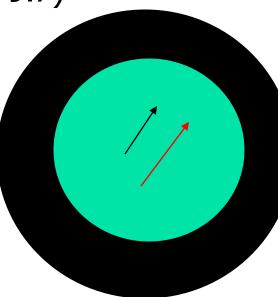
$$\frac{d\sigma_{+-}}{d\sigma_{++}} = \frac{tg^2(\frac{\phi}{2})}{(2\gamma - \gamma^{-1})^2}$$

Gyromagnetic and Gravigyromagnetic ratios

- Free particles coincide
- $P+q|T^{mn}|P-q> = P^{m}<P+q|J^{n}|P-q>/e$ up to the terms linear in q
- Gravitomagnetic g=2 for any spin
- Special role of g=2 for ANY spin (asymptotic freedom for vector bosons)
- Should Einstein know about PNEP, the outcome of his and de Haas experiment would not be so surprising
- Recall also g=2 for Black Holes. Indication of "quantum" nature?!

Cosmological implications of PNEP

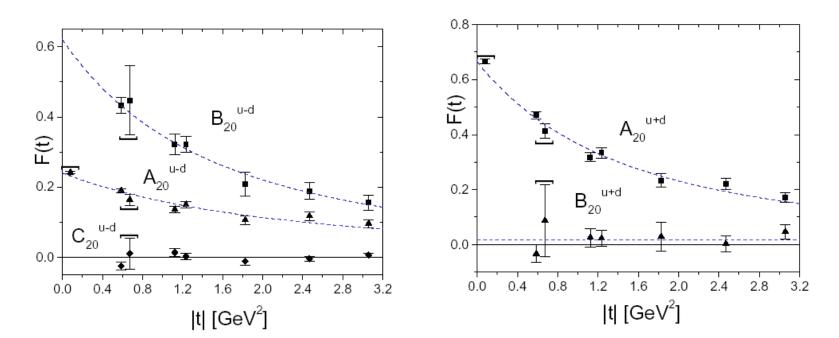
- Necessary condition for Mach's Principle (in the spirit of S.Weinberg's textbook-Section 9.7)
- Lense-Thirring inside massive rotating empty shell (=model of Universe)
- For flat "Universe" precession frequency equal to that of shell rotation
- Simple observation-Must be the same for classical and quantum rotators – PNEP!



More elaborate models - Tests for cosmology ?!

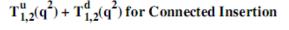
Generalization of Equivalence principle

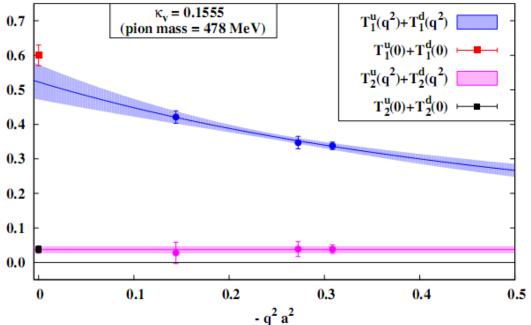
Various arguments: AGM ≈ 0 separately for quarks and gluons – most clear from the lattice (LHPC/SESAM)



More recent lattice study (M. Deka,...K.-F. Liu et al. Phys.Rev. D91 (2015) no.1, 014505)

Sum of u and d for Dirac (T1) and Pauli (T2) FFs





Extended Equivalence Principle=Exact EquiPartition

- In NLO pQCD violated (LF:S.Brodsky et al.)
- Reason in the case of ExEP- no smooth transition for zero fermion mass limit (Milton, 71)
- Conjecture (O.T., 2001 prior to lattice data) – valid in NP QCD – zero quark mass limit is safe due to chiral symmetry breaking
- Gravityproof confinement?! Nucleons do not break even by black holes?! Match BH complementarity?! "GeV Gravity"?
- Support by recent observation of smallness of EP-forbidden "Cosmological Constant"

Exact Equipartition and Pivot

- Important notion introduced by C. Lorce to relate transverse spin SR's of Ji&Yuan and Leader et al.
- Naïve interpretation of ExEP: common (approximately, averagely) pivot for quarks and gluons:
- $< J_{T(q,G)} > = < x_0 > < P_{L(q,G)} >$
- Can this be satisfied for some of pivot choices?

Quadrupole formfactor: Inflation and annihilation

Quadrupole gravitational FF

$$\langle P+q/2|T^{\mu\nu}|P-q/2\rangle = C(q^2)(g^{\mu\nu}q^2-q^{\mu}q^{\nu})+\dots$$

Vacuum – Cosmological Constant

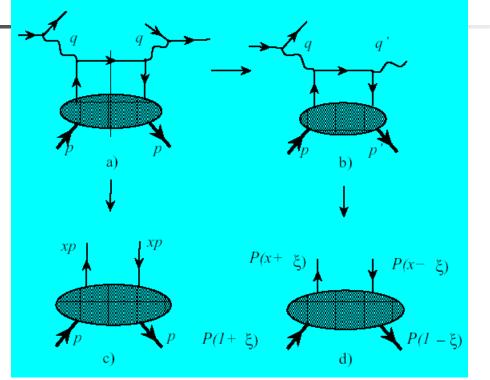
 $\langle 0|T^{\mu\nu}|0\rangle = \Lambda g^{\mu\nu}$

2D effective CC – negative in scattering, positive in annihilation

 $\Lambda = C(q^2)q^2$

- Similarity of inflation and Schwinger pair production Starobisnky, Zel'dovich
- Was OUR Big Bang resulting from one graviton annihilation at extra dimensions??! Version of "ekpyrotic" ("pyrotechnic") universe
- Traceless+Trace =
- M_I: (3/4+1/4) X.Ji'96
- M_{Gr}: (3/2-1/2) OT'99 ("Antigravity": seen in trace part of Einstein Eqs)
- Access: D-term in GPDs

Way to D-term: cf QCD Factorization for DIS and DVCS (AND VM production)



Manifestly spectral

$$\mathcal{H}(x_B) = \int_{-1}^{1} dx \frac{H(x)}{x - x_B + i\epsilon}$$

• Extra dependence on ξ $\mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,\xi)}{x-\xi+i\epsilon}$,

Unphysical regions

DIS : Analytical function – polynomial in $1/x_B$ if $1 \le |X_B|$

$$H(x_B) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

- DVCS additional problem of analytical continuation of H(x,ξ)
- Solved by using of Double Distributions
 Radon transform

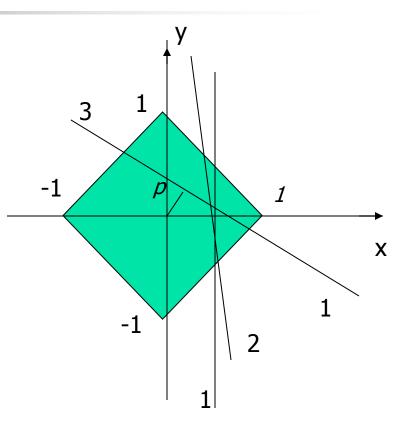
$$H(z,\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy (F(x,y) + \xi G(x,y)) \delta(z-x-\xi y)$$

Double distributions and their integration

- Slope of the integration lineskewness
- Kinematics of DIS: $\xi = 0$

("forward") - vertical line (1)

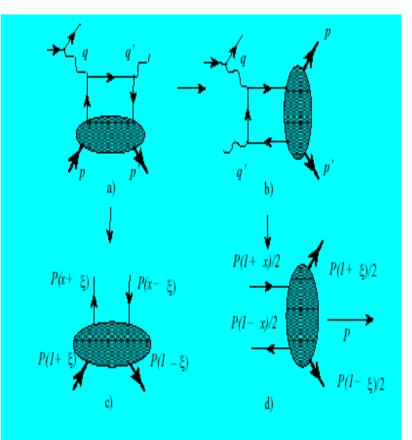
- Kinematics of DVCS: ξ <1
 line 2
- Line 3: ξ > 1 unphysical region - required to restore DD by inverse Radon transform: tomography



$$\begin{split} f(x,y) &= -\frac{1}{2\pi^2} \int_0^\infty \frac{dp}{p^2} \int_0^{2\pi} d\phi |\cos\phi| (H(p/\cos\phi + x + ytg\phi, tg\phi) - H(x + ytg\phi, tg\phi)) = \\ &= -\frac{1}{2\pi^2} \int_{-\infty}^\infty \frac{dz}{z^2} \int_{-\infty}^\infty d\xi (H(z + x + y\xi, \xi) - H(x + y\xi, \xi)) \end{split}$$

Crossing for DVCS and GPD

- DVCS -> hadron pair production in the collisions of real and virtual photons
- GPD -> Generalized
 Distribution Amplitudes
- Duality between s and t channels (Polyakov,Shuvaev, Guzey, Vanderhaeghen)



GDA -> back to unphysical regions for DIS and DVCS

Recall DIS

$$H(x_B) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x) \frac{x^n}{x_B^{n+1}}$$

Non-positive powers
 of X_B

$$H(\xi) = -\int_{-1}^{1} dx \sum_{n=0}^{\infty} H(x,\xi) \frac{x^{n}}{\xi^{n+1}}$$

DVCS

- Polynomiality (general property of Radon transforms): moments integrals in *x* weighted with *xⁿ* are polynomials in 1/ ξ of power *n+1*
- As a result, analyticity is preserved: only non-positive powers of ξ appear

Holographic property (OT'05)

->

Factorization Formula

$$\mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,\xi)}{x - \xi + i\epsilon}$$

 Analyticity -> Imaginary part -> Dispersion relation:

$$\mathcal{H}(\xi) = \int_{-1}^{1} dx \frac{H(x,x)}{x - \xi + i\epsilon}$$

$$\Delta \mathcal{H}(\xi) \equiv \int_{-1}^{1} dx \frac{H(x,x) - H(x,\xi)}{x - \xi + i\epsilon}$$

 "Holographic" equation (DVCS AND VM)

$$=\sum_{n=1}^{\infty}\frac{1}{n!}\frac{\partial^n}{\partial\xi^n}\int_{-1}^1H(x,\xi)dx(x-\xi)^{n-1}=const$$

Holographic property - II

Directly follows from double distributions

$$H(z,\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy (F(x,y) + \xi G(x,y)) \delta(z-x-\xi y)$$

 Constant is the SUBTRACTION one - due to the (generalized) Polyakov-Weiss term G(x,y)

$$\Delta \mathcal{H}(\xi) = \int_{-1}^{1} dx \int_{|x|-1}^{1-|x|} dy \frac{G(x,y)}{1-y}$$

$$= - \left(\int_{-\xi}^{\xi} dx \frac{D(x/\xi)}{x - \xi + i\epsilon} = \int_{-1}^{1} dz \frac{D(z)}{z - 1} = const \right)$$

Holographic property - III

- 2-dimensional space -> 1-dimensional section!
- Momentum space: any relation to holography in coordinate space ?!

• Strategy (now adopted) of GPD's studies: start at diagonals (through SSA due to imaginary part of DVCS $x = -\xi$ amplitude) and restore by making use of dispersion relations + subtraction constants

x= *E*

Analyticity of Compton amplitudes in energy plane (Anikin,OT'07)

Finite subtraction implied

$$\operatorname{Re}\mathcal{A}(\nu, Q^{2}) = \frac{\nu^{2}}{\pi} \mathcal{P} \int_{\nu_{0}}^{\infty} \frac{d\nu'^{2}}{\nu'^{2}} \frac{\operatorname{Im}\mathcal{A}(\nu', Q^{2})}{(\nu'^{2} - \nu^{2})} + \Delta \qquad \Delta = 2 \int_{-1}^{1} d\beta \frac{D(\beta)}{\beta - 1}$$
$$\Delta_{\operatorname{CQM}}^{p}(2) = \Delta_{\operatorname{CQM}}^{n}(2) \approx 4.4, \qquad \Delta_{\operatorname{latt}}^{p} \approx \Delta_{\operatorname{latt}}^{n} \approx 1.1$$

- Numerically close to Thomson term for real proton (but NOT neutron) Compton Scattering!
- Duality (sum of squares vs square of sum; proton: 4/9+4/9+1/9=1)?!

From D-term to pressure

- Inverse -> 1st moment (model)
 Kinematical factor: weighted pressure $C \sim (= 0)$ M.Polyakov'03 $T^Q_{\mu\nu}(\vec{r},\vec{s}) = \frac{1}{2E} \int \frac{d^3\Delta}{(2\pi)^3} e^{i\vec{r}\cdot\vec{\Delta}} \langle p', S' | \hat{T}^Q_{\mu\nu}(0) | p, S \rangle$ $T_{ij}(\vec{r}) = s(r) \left(\frac{r_i r_j}{r^2} \frac{1}{3} \delta_{ij} \right) + p(r) \delta_{ij}$
- Justification: (Fourier inversed) consistency principle for Born gravitational scatterring? 2D<->3D?

The pressure distribution inside the proton

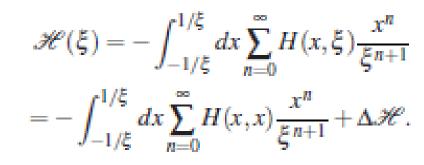
LETTER

V. D. Burkert¹*, L. Elouadrhiri¹ & F. X. Girod¹ 15 Repulsive 10 pressure r²p(r) (×10⁻² GeV fm⁻¹) 5 0 Confining pressure -5 0.2 0.4 0.6 0.8 1.2 1.6 0 1.0 1.4 1.8 2.0

r (fm)

Gravitational formfactors and pressure in hadron pairs production

- Back to GDA region
- -> moments of H(x,x) define the coefficients of powers of cosine!- 1/ξ
- Higher powers of cosine in t-channel – threshold in s -channel
- Larger for pion than for nucleon pairs because of less fast decrease at x ->1
- Stability defines the sign of GDA



Quantum roots of classical stability

GPDs

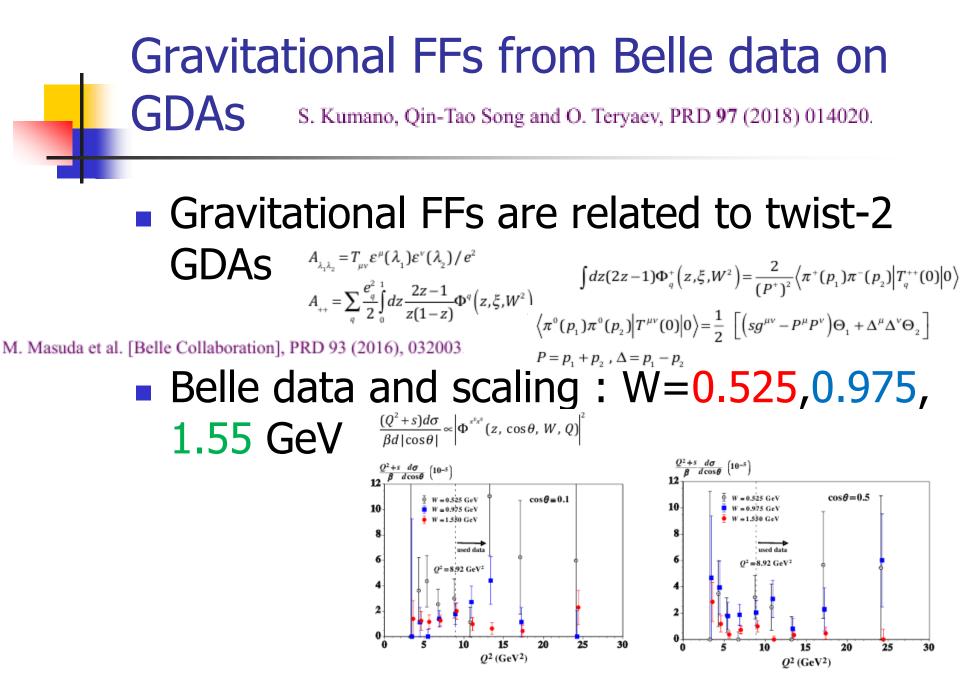
$$\Delta \mathcal{H}(\xi) \equiv \int_{-1}^{1} dx \frac{H(x,x) - H(x,\xi)}{x - \xi + i\epsilon}$$

$$= - \left(\int_{-\xi}^{\xi} dx \frac{D(x/\xi)}{x-\xi+i\epsilon} = \int_{-1}^{1} dz \frac{D(z)}{z-1} = const \right)$$

 Sufficient condition: positive (because of forward limit!) H is a decreasing function of 3 at any x **GDA'S** $H(z,\xi) = sign(\xi)\Phi(\frac{z}{\xi},\frac{1}{\xi})$

$$\begin{aligned} \mathscr{H}(\xi) &= -\int_{-1/\xi}^{1/\xi} dx \sum_{n=0}^{\infty} H(x,\xi) \frac{x^n}{\xi^{n+1}} \\ &= -\int_{-1/\xi}^{1/\xi} dx \sum_{n=0}^{\infty} H(x,x) \frac{x^n}{\xi^{n+1}} + \Delta \mathscr{H}. \end{aligned}$$

- Positivity of GDA balance between unitarity and stability
- Soft PION theorem positivity of DA!?



Phase shifts and resonances

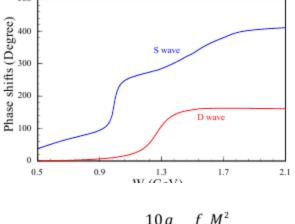
Leading harmonics

 $\sum_{q} \Phi_{q}^{+}(z,\xi,W^{2}) = 18n_{f}z(1-z)(2z-1)[B_{10}(W) + B_{12}(W)P_{2}(2\xi-1)]$ $= 18n_{f}z(1-z)(2z-1)[\tilde{B}_{10}(W) + \tilde{B}_{12}(W)P_{2}(\cos\theta)]$

$$\tilde{B}_{10}(W) = \overline{B}_{10}(W)e^{i\delta_0}$$
, $\tilde{B}_{12}(W) = \overline{B}_{12}(W)e^{i\delta_2}$

S/D shifts

f₀(500), f₂(1270) contributions



$$\overline{B}_{12}(W) = \beta^2 \frac{10g_{f_2\pi\pi}f_{f_2}M_{f_2}^2}{9\sqrt{2}\sqrt{(M_{f_2}^2 - W^2)^2 - \Gamma_{f_2}^2M_{f_2}^2}}$$
$$\overline{B}_{10}(W) = \frac{5g_{f_0\pi\pi}f_{f_0}}{3\sqrt{2}\sqrt{(M_{f_0}^2 - W^2)^2 - \Gamma_{f_0}^2M_{f_0}^2}}$$

Fits and results

 $\Phi_{a}^{+}(z,\xi,W^{2}) = N_{b}z^{a}(1-z)^{a}(2z-1)[\tilde{B}_{10}(W) + \tilde{B}_{12}(W)P_{2}(\cos\theta)]$ • Collection $\tilde{B}_{10}(W) = \left[\frac{-3+\beta^2}{2}\frac{5R_{\pi}}{9}F_h(W^2) + \frac{5g_{f_0\pi\pi}f_{f_0}}{3\sqrt{2}\sqrt{(M_{f_0}^2 - W^2)^2 - \Gamma_{f_0}^2M_{f_0}^2}}\right]e^{i\delta_0}$ $\tilde{B}_{12}(W) = [\beta^2 \frac{5R_{\pi}}{9} F_{h}(W^2) + \beta^2 \frac{10g_{f_2\pi\pi}f_{f_2}M_{f_2}^2}{9\sqrt{2}\sqrt{(M_{f_1}^2 - W^2)^2 - \Gamma_{f_1}^2 M_{f_2}^2}}]e^{i\delta_2}$ $F_{h}(W^{2}) = \frac{1}{\left[1 + \frac{W^{2} - 4m_{\pi}^{2}}{\Lambda^{2}}\right]^{n-1}}$

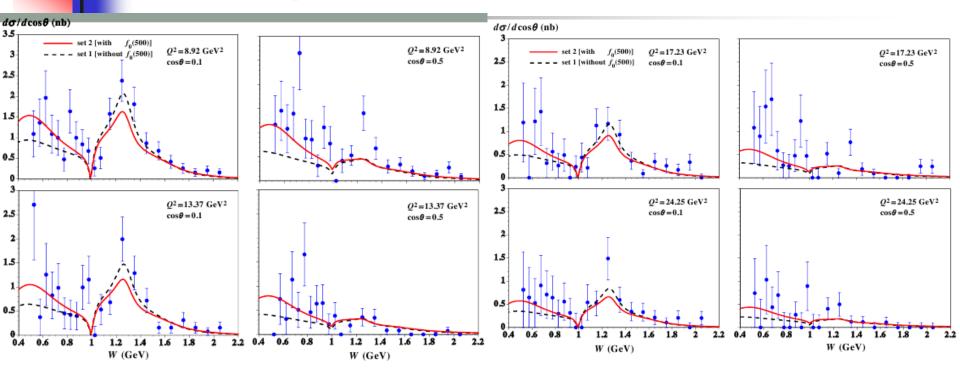
Best fit with (2) and without (1) f_0

NOF

	Set 1	Set 2
α	0.801±0.042	1.157± 0.132
Λ	1.602±0.109	1.928±0.213
а	3.878± 0.165	3.800± 0.170
b	0.382± 0.040	0.407± 0.041
f _{f0}		0.0184± 0.034
	$\chi^{2} = 1.22$	$\chi^{2} = 1.09$

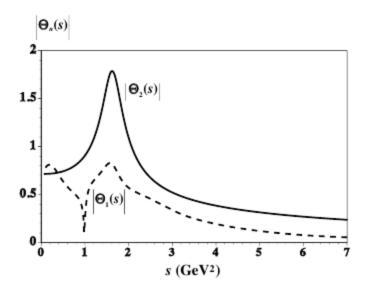
NOF

Description of data



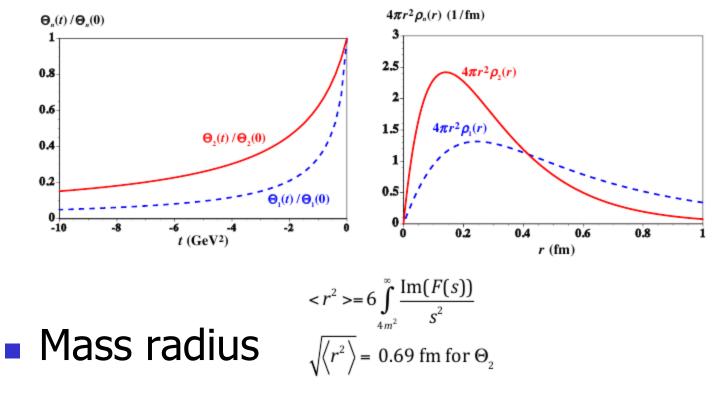


Resonance structure in pressure – related Θ₁



Time-like -> space-like

Dispersion relation and Fourier transform



Spin 1 EMT and inclusive processes

- Forward matrix element -> density matrix
- Contains P-even term: tensor polarization S ^{αβ}
- Symmetric and traceless: correspond to (average) shear forces
- For spin ½: P-odd vector polarization requires another vector (q) to form vector product

SUM RULES

- Efremov,OT'81 : zero sum rules:
- Current conservation: 1st moment: also in parton model by Close and Kumano (90)
- EMT conservation: 2^{nd} moment (forward analog of Ji's SR: AGM = $<A_T>=0$)
- Average shear force (compensated between quarks and gluons)
- Gravity and (Ex)EP (zero average shear separately for quarks and gluons) – OT'09

Manifestation of post-Newtonian (Ex)EP for spin 1 hadrons

• Tensor polarization coupling of EMT to spin in forward matrix elements inclusive processes $A_T = \frac{\sigma_+ + \sigma_- - 2\sigma_0}{3\bar{\sigma}}$

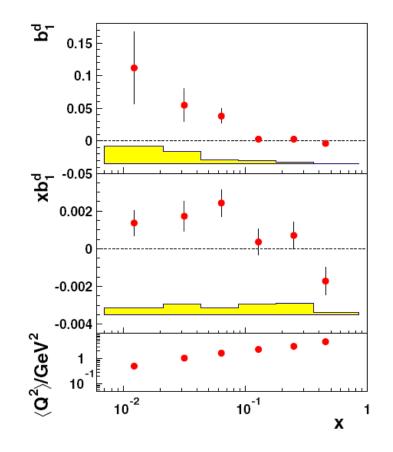
$$\begin{split} \langle P, S | \bar{\psi}(0) \gamma^{\nu} D^{\nu_1} \dots D^{\nu_n} \psi(0) | P, S \rangle_{\mu^2} &= i^{-n} M^2 S^{\nu\nu_1} P^{\nu_2} \dots P\nu_n \int_0^1 C_q^T(x) x^n dx \\ \sum_q \langle P, S | T_i^{\mu\nu} | P, S \rangle_{\mu^2} &= 2 P^{\mu} P^{\nu} (1 - \delta(\mu^2)) + 2 M^2 S^{\mu\nu} \delta_1(\mu^2) \\ \langle P, S | T_q^{\mu\nu} | P, S \rangle_{\mu^2} &= 2 P^{\mu} P^{\nu} \delta(\mu^2) - 2 M^2 S^{\mu\nu} \delta_1(\mu^2) \end{split}$$

 $(x)x^n dx$ (AVE.OT'91.93)

$$\sum_{q} \int_{0}^{1} C_{i}^{T}(x) x dx = \delta_{1}(\mu^{2}) = 0 \text{ for ExEP}$$

HERMES – data on tensor spin structure function PRL 95, 242001 (2005)

- Isoscalar target proportional to the sum of u and d quarks – combination required by (Ex)EP
- Second moments compatible to zero better than the first one (collective tensor polarized glue << sea)



Where else to test?

EIC

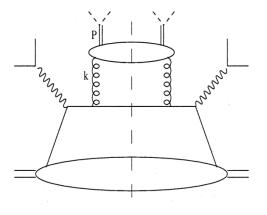
- DY@J-PARC
- ET'81-any hard process ("multimessenger")
- Possibility: hadronic tensor SSA@NICA

Fragmentation functions

Tensor polarized fragmentation functions: (Szvmanowski, Schaefer,

OT′99)

A. Schäfer et al. / Physics Letters B 464 (1999) 94-100



 Suggestion'21: zero SRs (analogous to momentum SR) may probe the (Ex)EP for hadrons inside partons (EIC: gluons)

More on vector mesons and ExEP

- J=1/2 -> J=1. QCD SR/model/lattice calculation of Rho's AMM gives g close to 2 (g=2 exactly in AdS QCD).
- Why?
- Maybe because of similarity of moments and ExEP
- g-2=<E_u(x)>; B=<xE_u(x)>
- Directly for charged Rho (combinations like p+n for nucleons unnecessary!). Not reduced to non-extended EP: Gluons momentum fraction sizable

EP: Where is the fastest possible rotation and acceleration?

- Non-central heavy ion collisions (Angular velocity ~ c/Compton wavelength) $\Omega \sim \frac{c}{\lambda_n} = \frac{m_p c^2}{\hbar}$
- ~25 orders of magnitude faster than Earth's rotation $\eta_{\text{rot}} = \frac{\Omega}{\omega_{\oplus}} = \frac{c}{R_A} \cdot \frac{T_{\oplus}}{2\pi} = \frac{1}{2\pi} \cdot \frac{cT_{\oplus}}{R_A} \approx 10^{27}$
- Differential rotation vorticity
- P-odd :May lead to various P-odd effects (Chiral magnetic/vortical effects)
- Acceleration: even larger ratio with the gravity of Earth

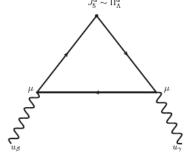
$$\eta_{\rm acc} = \frac{c}{R_A} \cdot \frac{c}{g_{\oplus}} = \eta_{\rm rot} \frac{2\pi c}{T_{\oplus} g_{\oplus}} \approx 10^{30} \qquad \eta_{\rm acc} = \frac{c}{R_A} \cdot \frac{c}{g_{\oplus}} = \frac{c^2}{v_{\oplus}^2} \cdot \frac{R_{\oplus}}{R_A}$$

Effective field theory: Anomalies

4-Velocity is also a GAUGE FIELD (V.I. Zakharov et al)

 $e_j A_\alpha J^\alpha \Rightarrow \mu_j V_\alpha J^\alpha$

- Triangle anomaly leads to polarization of quarks and hyperons (Rogachevsky, Sorin, OT '10)
- Analogous to anomalous gluon contribution to nucleon spin (Efremov,OT'88)



 4-velocity instead of gluon field potential and vorticity -----//-----(chromo)magnetic field strength!

STAR, Nature 548 (2017) 62-65

Observable for AVE: polarization

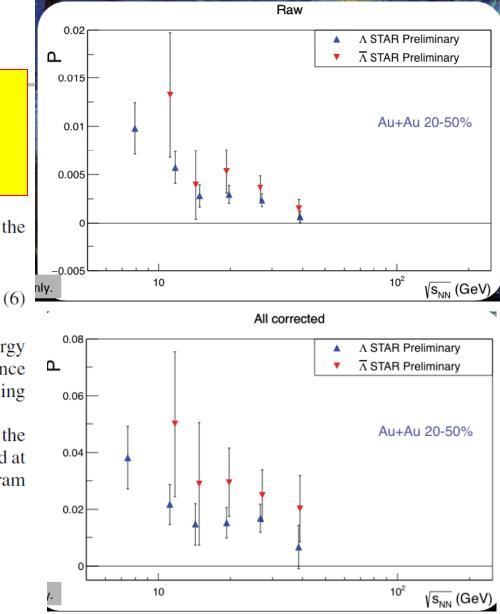
O. Rogachevsky, A. Sorin, O. Teryaev Chiral vortaic effect and neutron asymmetries in heavy-ion collisions PHYSICAL REVIEW C 82, 054910 (2010)

One would expect that polarization is proportional to the anomalously induced axial current [7]

$$j_A^{\mu} \sim \mu^2 \left(1 - \frac{2\mu n}{3(\epsilon + P)} \right) \epsilon^{\mu\nu\lambda\rho} V_{\nu} \partial_{\lambda} V_{\rho},$$

where *n* and ϵ are the corresponding charge and energy densities and *P* is the pressure. Therefore, the μ dependence of polarization must be stronger than that of the CVE, leading to the effect's increasing rapidly with decreasing energy.

This option may be explored in the framework of the program of polarization studies at the NICA [17] performed at collision points as well as within the low-energy scan program at the RHIC.



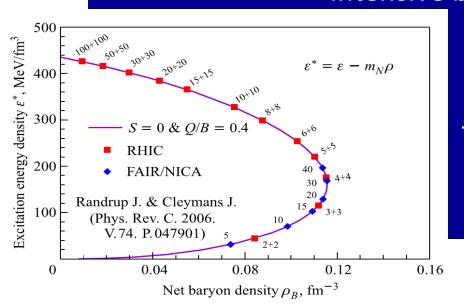
NICA (Nuclotron based Ion Colider fAcility) – the flagship project in HEP of Joint Institute for Nuclear Research (JINR)

Main targets of "NICA Complex":

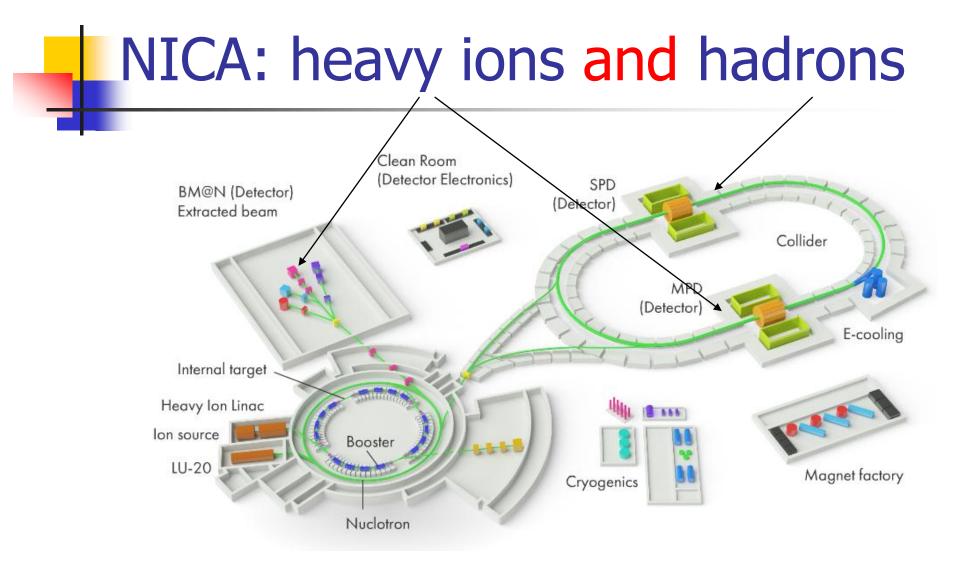
- study of hot and dense baryonic matter
- investigation of hadronic spin structure through various

polarization phenomena

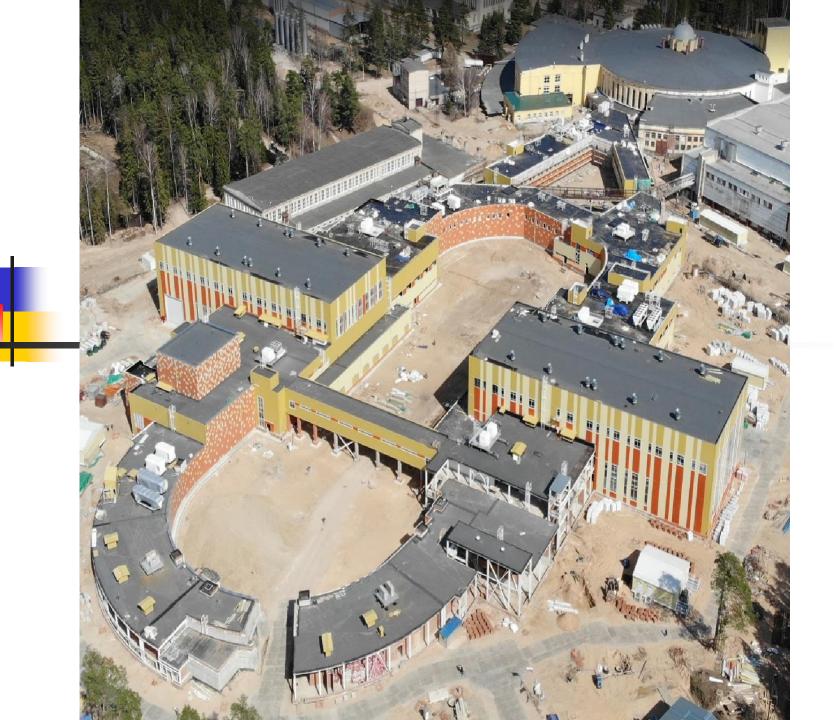
- development of accelerator facility for HEP @ JINR providing intensive beams of relativistic ions from p to Au



polarized protons and deuterons with energy up to $VS_{NN} = 11 \text{ GeV} (Au^{79+}, L \sim 10^{32} \text{ cm}^{-2} \text{ c}^{-1})$ $VS = 27 \text{ GeV} (p, L \sim 10^{32} \text{ cm}^{-2} \text{ c}^{-1})$





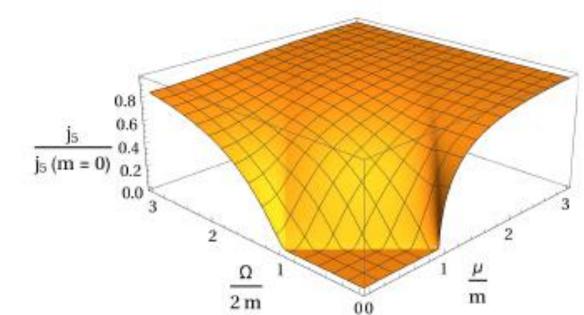


Why EP and rotating frame?

- Statistical approach (F. Becattini et al.; "Standard Model" for polarization): spin equilibrium in rotating frame
- Decrease with energy: explained by decrease of (relevant) hydrodynamic vorticity (Betz, Torrieri, Csernai, Becattini, Karpenko, Lisa,...)
- Interesting to compare with quantum measurement essential for EP: Landau&Lifshitz v. 5, Section 8 ("Law of entropy increasing"): possible relation of inequivalence of time directions due to quantum measurements
- EP/quantum measurement/statistics interplay (recall history of Kobzarev&Okun publication)?!
- Cf.: EP violation (modification?) due to thermal effects (nonzero AGM: Buzzegoli, Kharzeev'21)

Comparison of approaches: Axial ("anomalous" without anomaly) current in TD approach: Vilenkin'82,...

- Prokhorov, Zakharov, OT'18:Threshold effects in chemical potential and angular velocity
- From equilibrated spin of massive hadrons to EFT for spin of massless quarks



Rotated and accelerated frame: Wigner function and Zubarev density operator

G. Prokhorov, V. Zakharov, OT '19:
 Imaginary chemical potential due to acceleration appears! (μ) = (μ) = (μ) / (2π)³

$$\begin{split} & \times \{n_F(E_p - \mu - g_w/2 + ig_a/2) \\ & - n_F(E_p - \mu + g_w/2ig_a/2) \\ & + n_F(E_p + \mu - g_w/2 + ig_w/2) \\ & - n_F(E_p + \mu + g_w/2 - ig_a/2)\} + \text{c.c.}, \end{split}$$

$$\rho = \frac{7\pi^2 T^4}{60} + \frac{T^2 a^2}{24} - \frac{17a^4}{960\pi^2} = 2 \int \frac{d^3 p}{(2\pi)^3} \left(\frac{|\mathbf{p}| + ia}{1 + e^{\frac{|\mathbf{p}|}{T} + \frac{ia}{2T}}} + \frac{|\mathbf{p}| - ia}{1 + e^{\frac{|\mathbf{p}|}{T} - \frac{ia}{2T}}}\right) + 4 \int \frac{d^3 p}{(2\pi)^3} \frac{|\mathbf{p}|}{e^{\frac{2\pi |\mathbf{p}|}{a}} - 1} \qquad (T > T_U) \quad \text{in red: modifications compared to the Wigner function}$$

In the first integral, the acceleration enters as an imaginary chemical potential ± ^{ia}/₂ [G.P., O. Teryaev, V. Zakharov, Phys. Rev. D 98, no. 7, 071901 (2018)].

Statistics vs geometry: Unruh effect (Becattini'18; Prokhorov, OT, Zakharov'19)

Results for energy density of thermal system in Minkowski space coincide with the early known for the space with conical singularity (e.g. cosmic strings) $\pi^{2}T^{4} = T^{2}|a|^{2} = 11|a|^{4}$

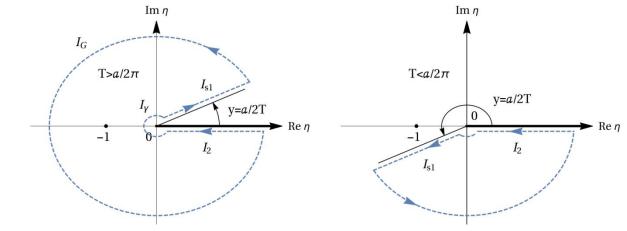
$$c_V = \frac{\mu_s^2 + \mu_A^2}{2\pi^2} + \frac{T^2}{6}, \quad Q_5^s = N_c \int d^3x \, c_V \gamma^2 \epsilon^{ijk} v_i \partial_j v_k$$

 $\rho_{s=0} = \frac{\pi^2 T^4}{30} + \frac{T^2 |a|^2}{12} - \frac{11|a|^4}{480\pi^2},$ $\rho_{s=1/2} = \frac{7\pi^2 T^4}{60} + \frac{T^2 |a|^2}{24} - \frac{17|a|^4}{960\pi^2}$

 Energy density turns to zero for T=T_U=a/(2π) (~"physical conditions of renormalization". also simple explanation of coefficient)

Instability for high accelerations

- Normally T>T_U
- Fast accelration without thermalization: instability



 $T_1 > T_U$

 $T_3=T_U$

- EP ~ fall to BH?
- Censorship: Origin for fast thermalization?

CONCLUSIONS

Equivalence principle: allows to study interplay of QCD and gravity

 Modern accelerators (LHC, RHIC, CEBAF EIC,FAIR,NICA... also "effective gravity" labs

Conclusions/Outlook

- EMT coupling
- Separate couplings of quarks and gluons to gravity: ExEP, pressure, shear, cosmological constant
- EP in QCD matter ("GeV gravity")
- Anomalous transport and polarization
- Unruh radiation

EP-I/EPII intersections

OUTLOOK

Pressure, shear, EoS for hadrons

 Helicity flip (Relic neutrino, PTOLEMY, Dark matter)



Is D-term independent?

Fast enough decrease at large energy - $\operatorname{Re} \mathcal{A}(\nu) = \frac{\mathcal{P}}{\pi} \int_{\nu_{\star}}^{\infty} d\nu'^2 \frac{\operatorname{Im} \mathcal{A}(\nu')}{\nu'^2 - \nu^2} + C_0$ $C_0 = \Delta - \frac{\mathcal{P}}{\pi} \int_{-\infty}^{\infty} d\nu'^2 \frac{\mathrm{Im}\,\mathcal{A}(\nu')}{\nu'^2}$ $= \Delta + \mathcal{P} \int_{-1}^{1} dx \frac{H^{(+)}(x, x)}{x}.$ FORWARD limit of Holographic equation $C_0(t) = 2\mathcal{P} \int_{-1}^1 dx \frac{H(x, 0, t)}{x}$ $\Delta = \mathcal{P} \int_{-1}^{1} dx \frac{H^{(+)}(x, 0) - H^{(+)}(x, x)}{x}$ $=2\mathcal{P}\int_{-1}^{1}dx\frac{H(x,0)-H(x,x)}{x},$

"D – term" 30 years before...

- Cf Brodsky, Close, Gunion'72 (seagull ~ pressure) – but NOT DVMP
- D-term a sort of renormalization constant
- May be calculated in effective theory if we know fundamental one
- OR
- Recover through special regularization procedure (D. Mueller)?

ExEP and AdS/QCD

- Recent development calculation of Rho formfactors in Holographic QCD (Grigoryan, Radyushkin)
- Provides g=2 identically!
- Experimental test at time –like region possible

ExEP and Sivers function

- Sivers function process dependent (effective) one
- T-odd effect in T-conserving theory- phase
- FSI Brodsky-Hwang-Schmidt model
- Unsuppressed by M/Q twist 3
- Process dependence- colour factors
- After Extraction of phase relation to universal (T-even) matrix elements

ExEP and Sivers function -II

- Qualitatively similar to OAM and Anomalous Magnetic Moment (talk of S. Brodsky)
- Quantification : weighted TM moment of Sivers PROPORTIONAL to GPD E (OT'07, hep-ph/0612205): $xf_T(x): xE(x)$
- Burkardt SR for Sivers functions is then related to Ji's SR for E and, in turn, to Equivalence Principle

$$\sum_{q,G} \int dxx f_T(x) = \sum_{q,G} \int dxx E(x) = 0$$

ExEP and Sivers function for deuteron

- EEP smallness of deuteron Sivers function
- Cancellation of Sivers functions separately for quarks (before inclusion gluons)
- Equipartition + small gluon spin large longitudinal orbital momenta (BUT small transverse ones –Brodsky, Gardner)

Another relation of Gravitational FF and NP QCD (first reported at 1992: hep-ph/9303228)

- BELINFANTE (relocalization) invariance :
 decreasing in coordinate $M^{\mu,\nu\rho} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} J_{S\sigma}^5 + x^{\nu} T^{\mu\rho} x^{\rho} T^{\mu\nu}$ smoothness in momentum space $M^{\mu,\nu\rho} = x^{\nu} T_B^{\mu\rho} x^{\rho} T_B^{\mu\nu}$
- Leads to absence of massless
 pole in singlet channel U_A(1)
- $\epsilon_{\mu\nu\rho\alpha}M^{\mu,\nu\rho} = 0.$
- Delicate effect of NP QCD $(g_{\rho\nu}g_{\alpha\mu} g_{\rho\mu}g_{\alpha\nu})\partial^{\rho}(J_{5S}^{\alpha}x^{\nu}) = 0$
- Equipartition deeply $q^2 \frac{\partial}{\partial q^{\alpha}} \langle P|J_{5S}^{\alpha}|P+q \rangle = (q^{\beta} \frac{\partial}{\partial q^{\beta}} 1)q_{\gamma} \langle P|J_{5S}^{\gamma}|P+q \rangle$ related to relocalization $\langle P, S|J_{\mu}^{5}(0)|P+q, S \rangle = 2MS_{\mu}G_{1} + q_{\mu}(Sq)G_{2},$ $q^{2}G_{2}|_{0} = 0$ invariance by QCD evolution

Holography vs NLO

Depends on factorization scheme

 Special role of scheme preserving the coefficient function

 Nucleon as (scheme dependent) black hole – 3D information encoded in 2D

C vs Cbar (=∧)

- Cancellations of Cbars negative pressure
- Cf Chaplygin gas: (p=-A/Q) analog of cosmological constant
- Cancellation in vacuum; Pauli (divergent), Zel'dovich (finite)
- Flavour structure of pressure: DVMP!